

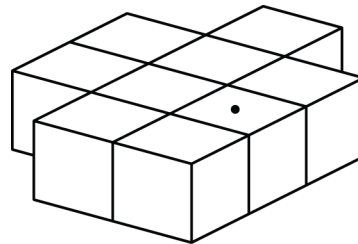
# Mathematica Centrum

Together, let's shape the mathematicians of the future

## THALES PREPARATORY TEST 2016 DETAILED SOLUTIONS

1. The base of a pyramid has 6 sides. In all, this pyramid has  $(6 + 1) \cdot 7$  vertices.
2. The expression  $400 < 398$  is false.
3. The difference between  $(7 \times 12) \cdot 84$  and  $(72 \div 8) \cdot 9$  is  $(84 - 9) \cdot 75$ .
4. A period of 8 weeks is equal to  $(8 \times 7) \cdot 56$  days. A period of  $(56 + 8) \cdot 64$  days represents more than 63 days.
5. The ten's digit of  $(428 - 348) \cdot 80$  is 8.
6. There are about  $(6 \times 30) \cdot 180$  days or a little less than  $(180 \div 7) \cdot 26$  weeks in a period of 6 months. You will go to the gym approximately  $(26 \times 5) \cdot 130$  times over a period of 6 months.

7. Nine blocks have been glued together, as shown in the diagram. There is only 1 block (the one with a dot) that has exactly 3 faces that have glue on them.

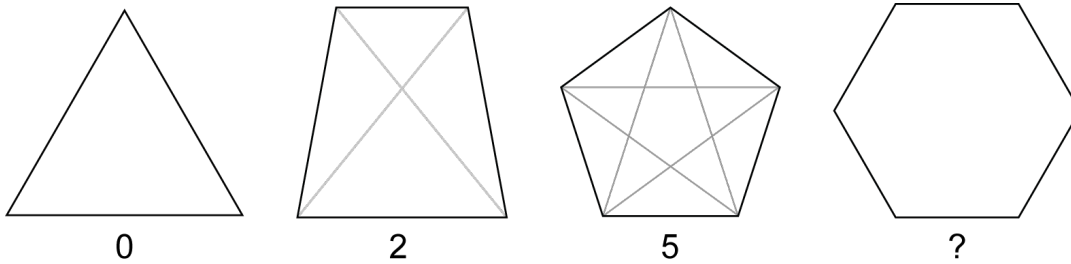


8. Mathew is  $X$  years old and Mathilda  $Y$  years old. The sum of their ages is presently  $X + Y$ . Three years ago, the sum of their ages was  $X + Y - 6$ .
9. From 1 to 100 there are 100 natural numbers. If we take away all 1-digit natural numbers (1 to 9) and the only 3-digit natural number (100), there is a total of  $(100 - 10) \cdot 90$  2-digit natural numbers.

X	9	10	7
3	<b>27</b>	30	21
<b>4</b>	36	<b>40</b>	<b>28</b>

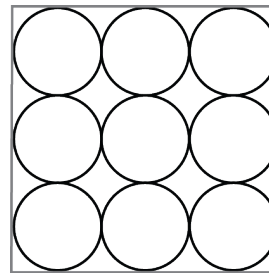
10. The expression that yields a sum that is even is  $12 + 14 + 55 + 33$ .
11. Mathilda rolls a dice 30 times. She should expect to get a 5  $(30 \div 6) \cdot 5$  times.
12. The number represented by a  $?$ , that has a value closest to 30 is, 28.
13. 3 hundreds  $(300) + 50$  ones  $+ 16$  tens  $(160)$  is equal to  $(300 + 50 + 160) \cdot 510$ .

14. 2 m (200 cm) + 1 dm (10 cm) + 5 cm is equal to (200 + 10 + 5) 215 cm.
15. There are 3 different ways (10 x \$2, 4 x \$5, and (2 x \$5 + 5 x \$2)) to make change for a \$20 bill if you were using \$5 bills and \$2 coins.
16. Zero diagonals can be drawn in a triangle. Two diagonals can be drawn in a quadrilateral, and 5 can be drawn in a pentagon. If you analyse closely these three numbers, you can see that they form a logical sequence. Indeed,  $0 + 2 = 2$ ,  $2 + 3 = 5$ . The number of diagonals that can be drawn in a hexagon is  $(5 + 4) 9$ .

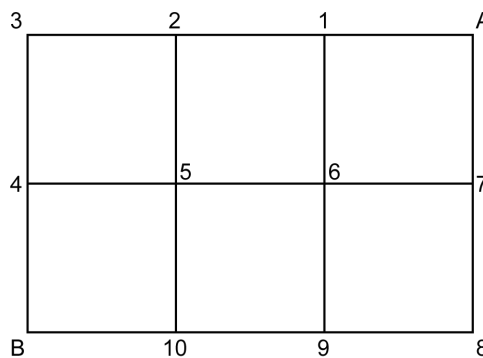


17. From  $N \times N = 1 + 2 + 3 + 4 + 3 + 2 + 1$ , we deduce that  $N \times N = 16 = 4 \times 4$  and that  $N = 4$ . The value of  $10 \times N$  is equal to  $(10 \times 4) 40$ .

18. Andrea can stack 4 balls on the 9 balls that form the base. On these 4 balls, she can stack one other ball. She will need  $(4 + 1) 5$  more balls to form this "pyramid".



19. There are 10 different 500 m routes (A-1-2-3-4-B, A-1-2-5-4-B, A-1-2-5-10-B, A-1-6-5-4-B, A-1-6-5-10-B, A-1-6-9-10-B, A-7-6-5-4-B, A-7-6-5-10-B, A-7-6-9-10-B, and A-7-8-9-10-B) to get from point A to point B.



20. Melissa has bought 5¢ and 10¢ stamps for a total of 55¢. If she were to buy the same number of 5¢ stamps, but twice the number of 10¢ stamps, it would cost her \$1.05. From these two premises, we can infer that the amount paid for the 10¢ stamps is  $(105¢ - 55¢) 50¢$ . The number of 10¢ stamps she has bought is  $(50¢ \div 10¢) 5$  and that of 5¢ is  $((55¢ - 50¢) \div 5¢) 1$ .